Introduction to Vector Diagrams



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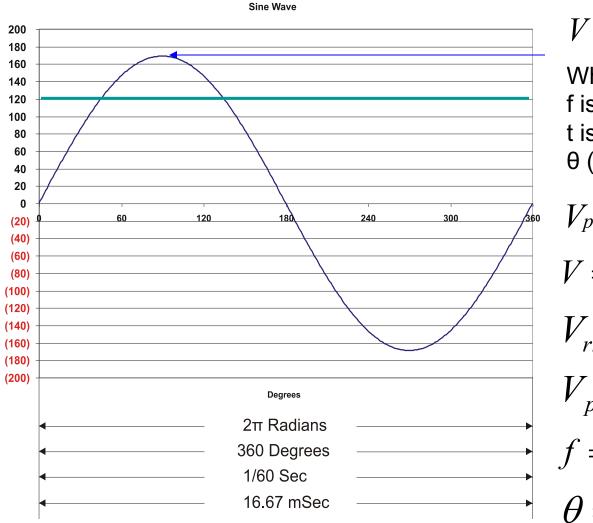
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AC Theory Review – Sine Wave



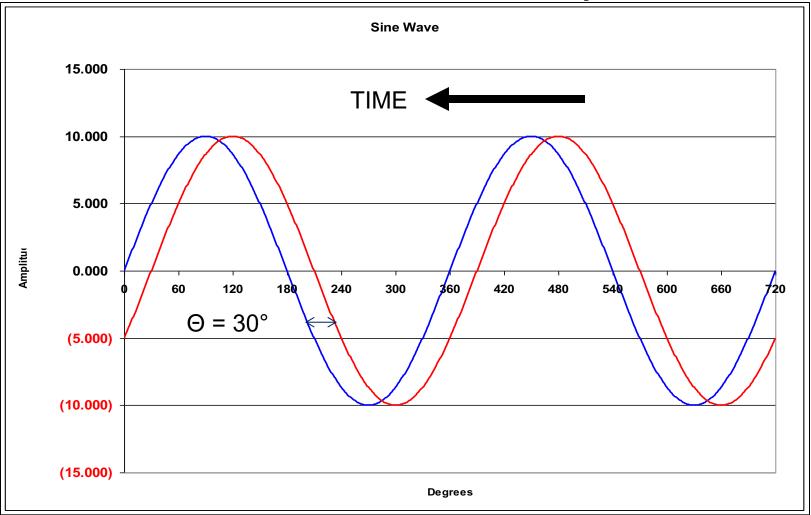
$$V = V_{pk} Sin(2\pi ft - \theta)$$

Where Vpk is peak voltage f is frequency t is time θ (theta) is phase

 $V_{pk} = \sqrt{2}V_{rms}$ $V = \sqrt{2}V_{rms}Sin(2\pi ft - \theta)$ $V_{rms} = 120V$ $V_{pk} = 169V$ f = 60Hz $\theta = 0^{\circ}$



Phase Relationship

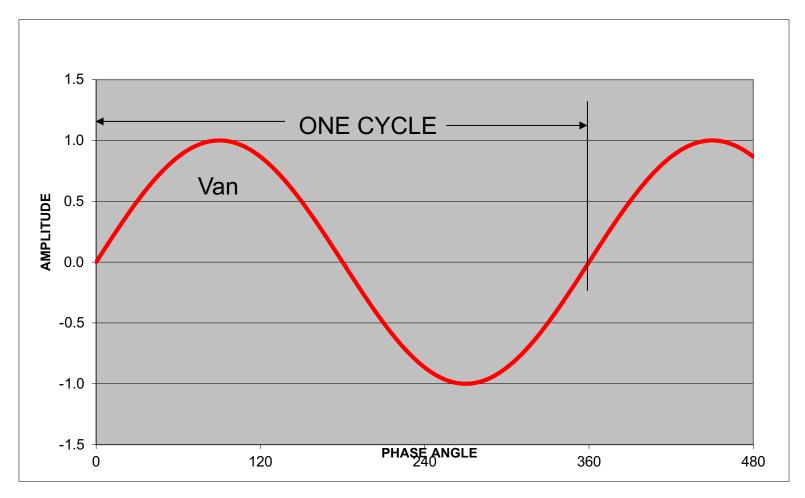


Current is lagging Voltage by 30°



Three Phase Theory

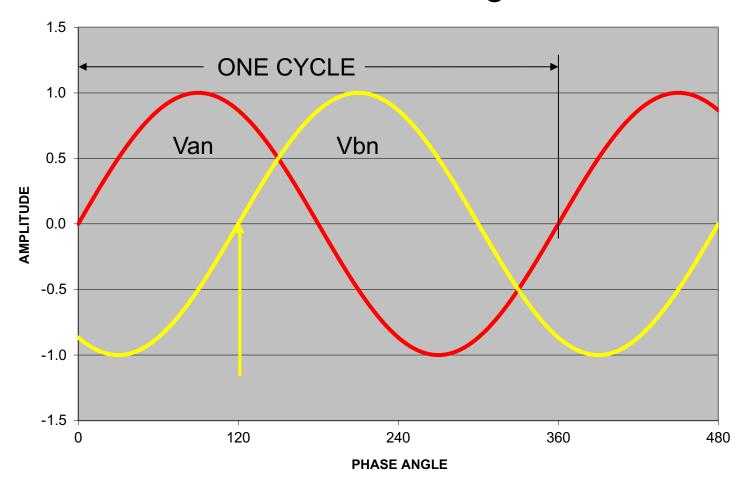
Single Phase - Voltage Plot





Three Phase Theory

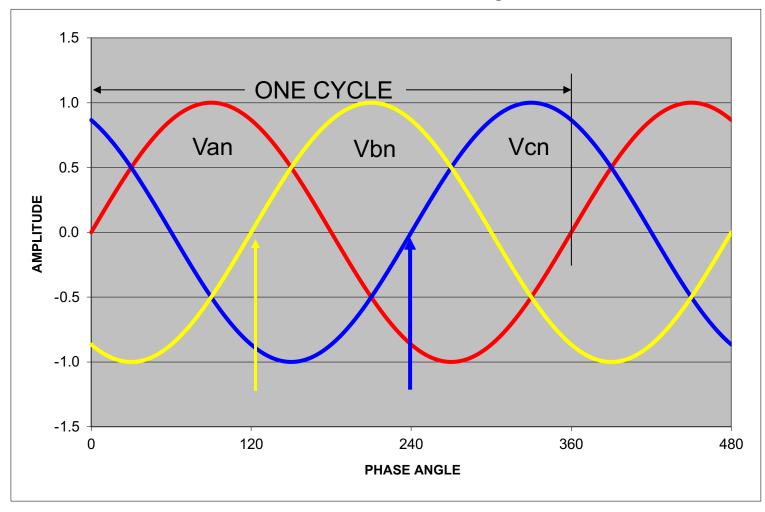
Two Phases - Voltage Plot





Three Phase Theory

Three Phase - Voltage Plot





Three Phase Power At the Generator

1.5 Van Vbn Vcn Three voltage vectors 1.0 each separated by 0.5 AMPLITUDE 0.0 -0.5 Peak voltages essentially equal. -1.0 -1.5 120 240 360 n

120°.

Most of what makes three phase systems seem complex is what we do to this simple picture in the delivery system and loads.

PHASE ANGLE



480

Three Phase Power Basic Concept – Phase Rotation

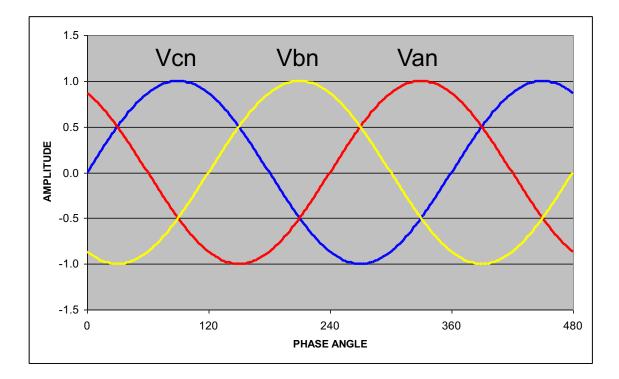
Phase Rotation:

The order in which the phases reach peak voltage.

There are only two possible sequences:

A-B-C (previous slide)

C-B-A (this slide)

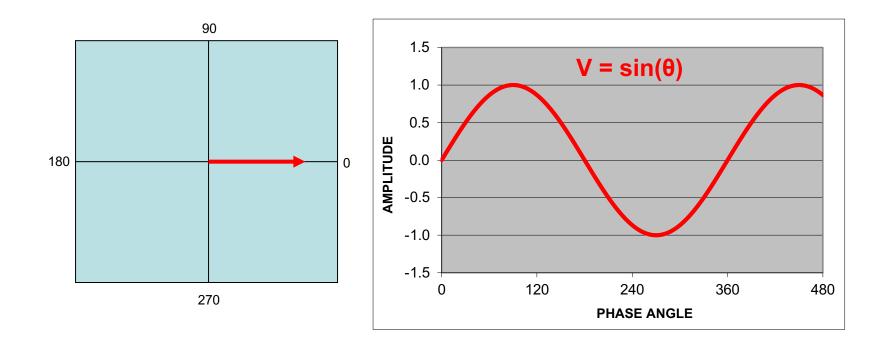


Phase rotation is important because the direction of rotation of a three phase motor is determined by the phase order.



Three Phase Theory Phasors and Vector Notation

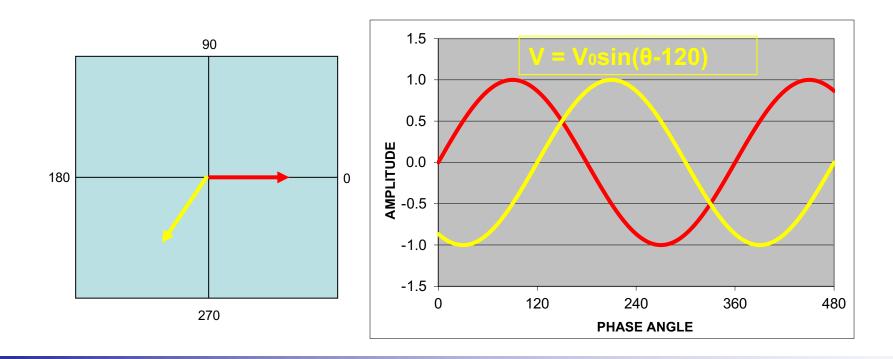
 Phasors are a graphical means of representing the amplitude and phase <u>relationships</u> of voltages and currents.





Three Phase Power Phasors and Vector Notation

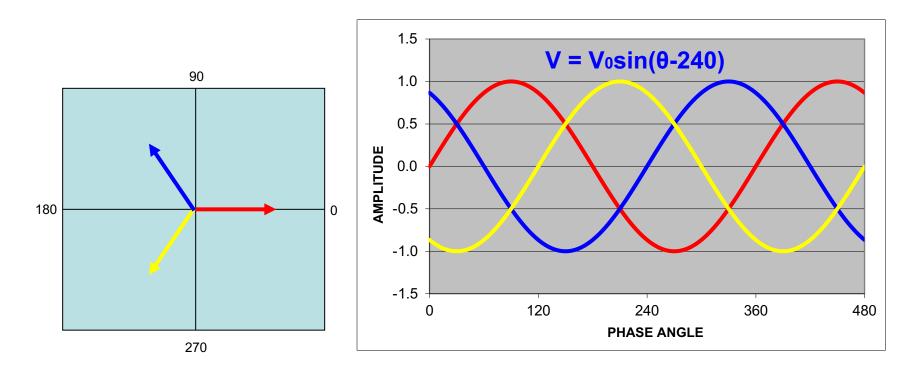
• As stated in the Handbook of Electricity Metering, by common consent, counterclockwise phase rotation has been chosen for general use in phasor diagrams.





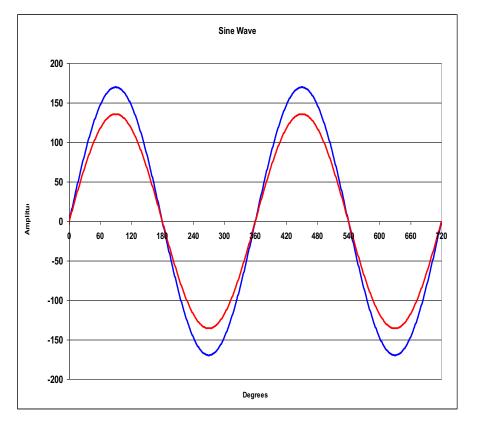
Three Phase Power Phasors and Vector Notation

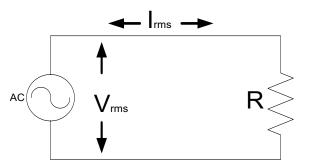
- The phasor diagram for a simple 3-phase system has three voltage phasors equally spaced at 120° intervals.
- Going clockwise the order is A B C.

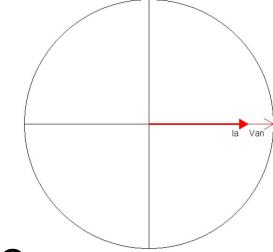




Resistive Load



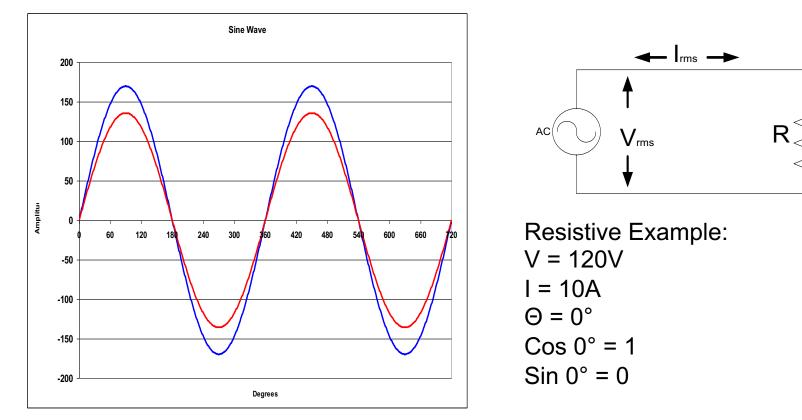




A purely resistive load has ZERO phase angle. The voltage and current vectors overlap.



Resistive Load

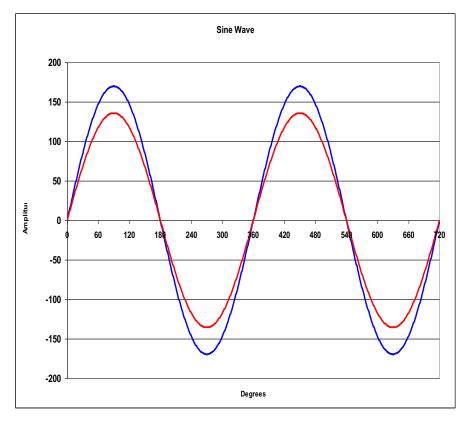


Active Power (W) = V I cos (θ) = 120 * 10 * 1 = 1200 W Reactive Power (VAR) = V I sin (θ) = 120 * 10 * 0 = 0 VAR Apparent Power (VA) = V I = 120 * 10 = 1200 VA

 $PF = W / VA = \cos(\theta) = 1$

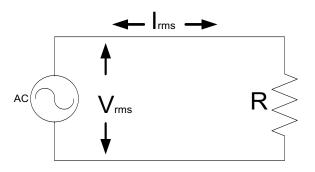


Resistive Load



A purely resistive load will:

- Only create Watts
- Create NO VARs
- Have a PF = 1 and phase angle of 0°

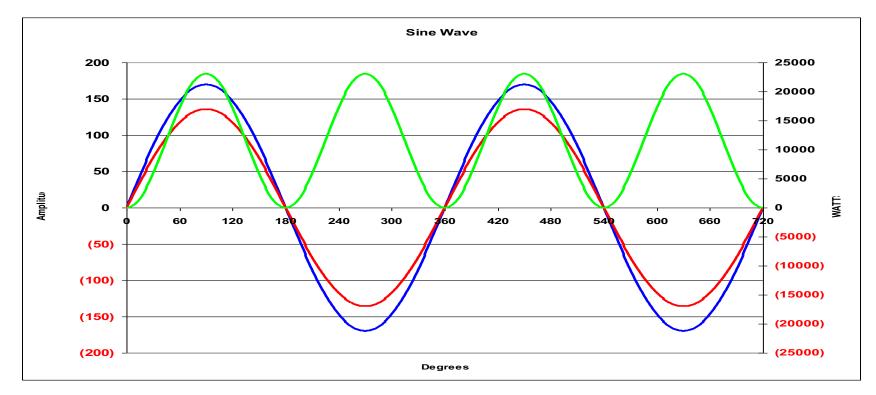






Resistive Load

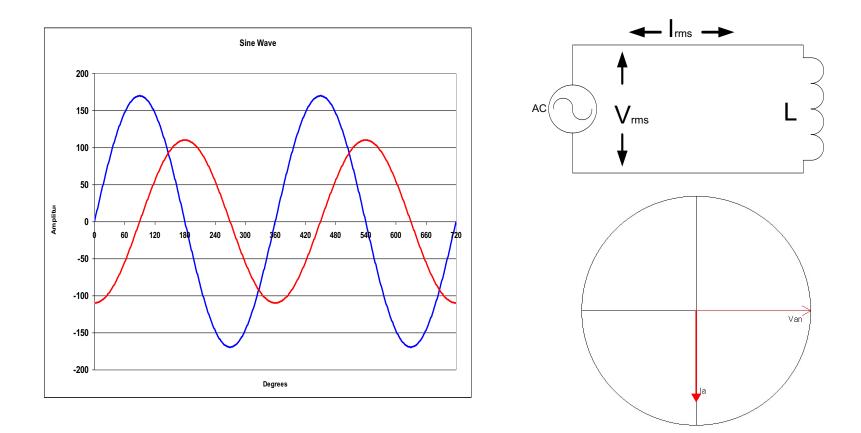
For a resistive load: $p = vi = 2VISin^2(\omega t) = VI(1 - Cos(2\omega t))$



A resistive load consumes only Watts, so the power will always be delivered (positive).



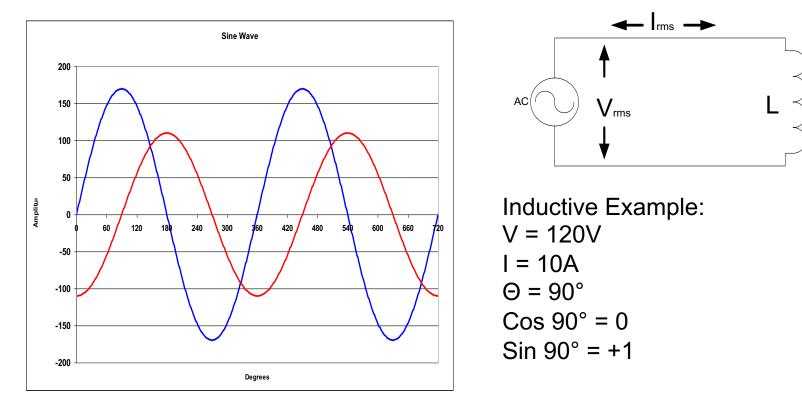
Inductive Load



A purely inductive load has +90° phase angle. Clockwise vectors are LAGGING as current lags voltage.



Inductive Load

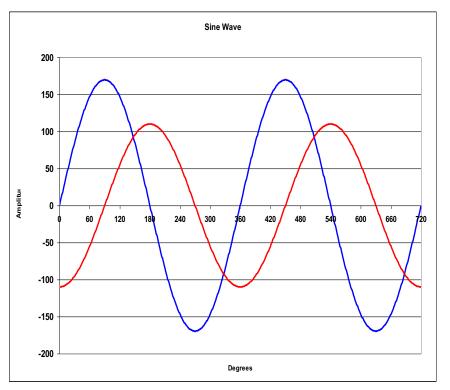


Active Power (W) = V I cos (θ) = 120 * 10 * 0 = 0 W Reactive Power (VAR) = V I sin (θ) = 120 * 10 * +1 = +1200 VAR Apparent Power (VA) = V I = 120 * 10 = 1200 VA

 $PF = W / VA = \cos(\theta) = 0$



Inductive Load



 $\begin{array}{c} \leftarrow I_{rms} \rightarrow \\ \uparrow \\ \downarrow \\ \downarrow \\ \end{array}$



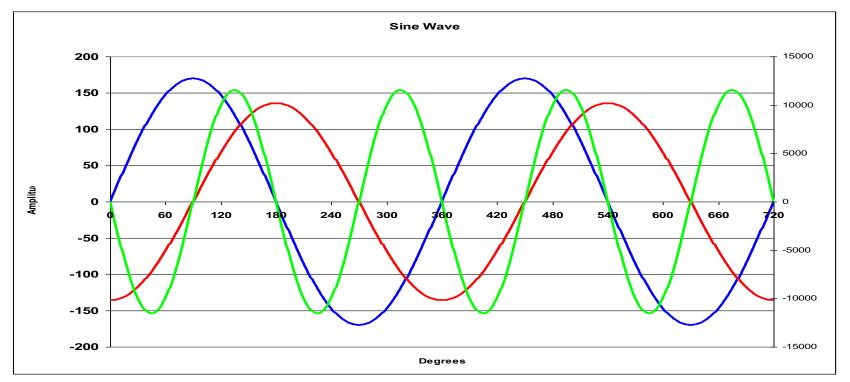
A purely inductive load will:

- Only create positive VARs
- Create NO Watts
- Have a PF = 0 and phase angle of 90° lagging



Inductive Load

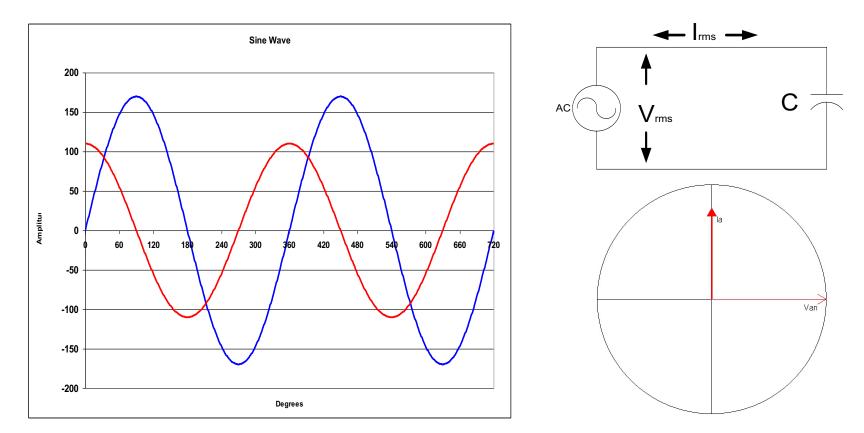
For an inductive load: $p = vi = 2VISin(\omega t)Sin(\omega t - 90) = -VISin(2\omega t)$



An inductive load consumes receives and delivers equal amounts of power, so the net active power (Watts) is ZERO And the reactive load is 100%!



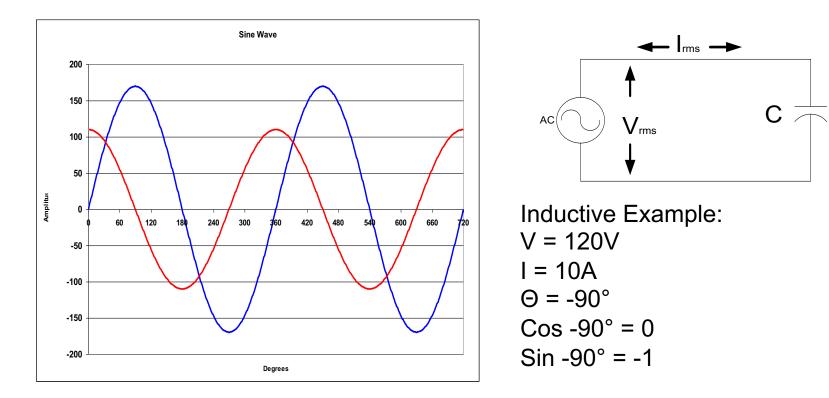
Capacitive Load



A purely capacitive load has -90° phase angle. Counter-clockwise vectors are LEADING as current leads voltage.



Capacitive Load

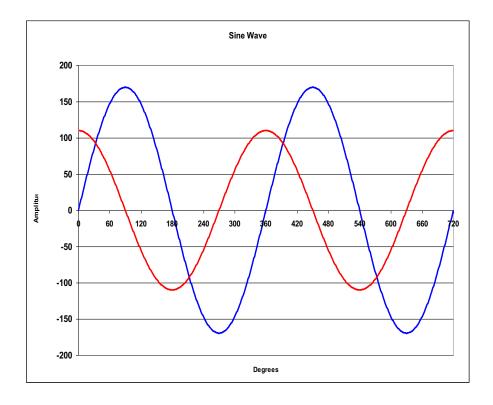


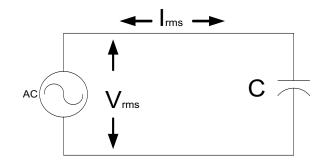
Active Power (W) = V I cos (θ) = 120 * 10 * 0 = 0 W Reactive Power (VAR) = V I sin (θ) = 120 * 10 * -1 = -1200 VAR Apparent Power (VA) = V I = 120 * 10 = 1200 VA

 $PF = W / VA = \cos(\theta) = 0$



Capacitive Load







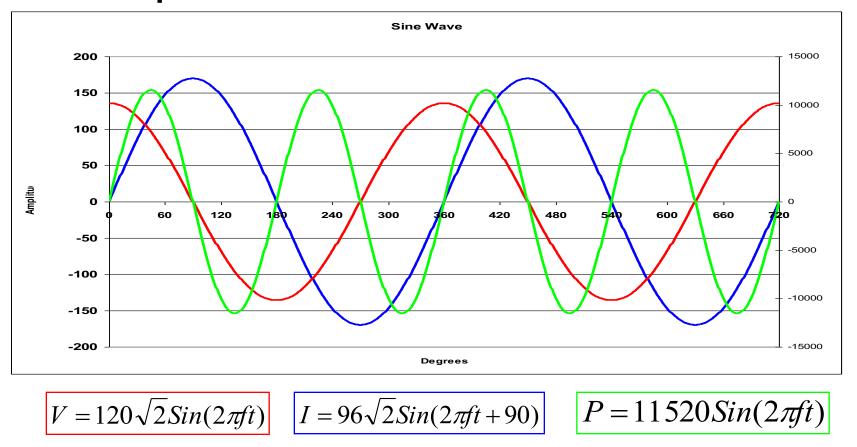
A purely capacitive load will:

- Only create negative VARs
- Create NO Watts
- Have a PF = 0 and phase angle of 90° leading



AC Theory – Instantaneous Power

For a capacitive load: $p = vi = 2VISin(\omega t)Sin(\omega t + 90) = VISin(2\omega t)$



P = 0 Watts



Inductance Vs Capacitance

- More inductance creates more VAR, less W, and lower PF
- Capacitance is added to an inductive load to reduce VAR, raise W, and raise PF
- Ideally, we want all loads to have a PF = 1





Power Factor, Watts, and VARs

For a 120V, 10A System

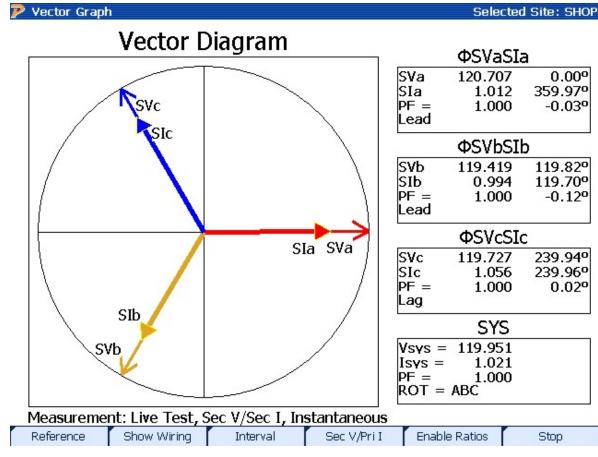
Phase Angle	PF	Watts	VAR	VA
0	1	1200 W	0 VAR	1200 VA
30	0.866	1039 W	600 VAR	1200 VA
60	0.5	600 W	1039 VAR	1200 VA

As PF gets closer to 1, the Watt value gets closer to the VA value! This means more real power is being consumed!



3 Phase, 4-Wire "Y" Service 0° = Unity Power Factor

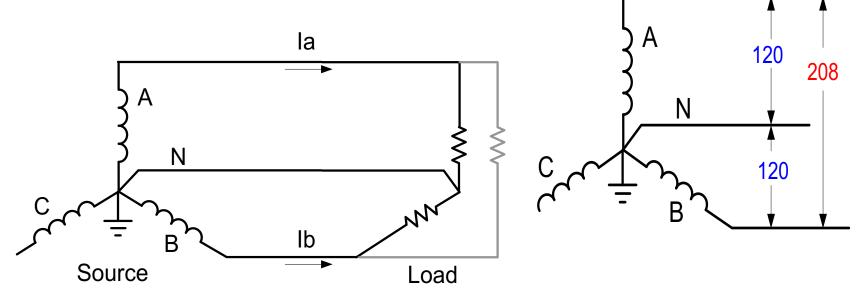
- Three Voltage Phasors
- 120° Apart
- Three Current Phasors
- Aligned with Voltage at PF=1





2 Phase, 3-Wire "Y" Service "Network Connection"

Single phase variant of the service.

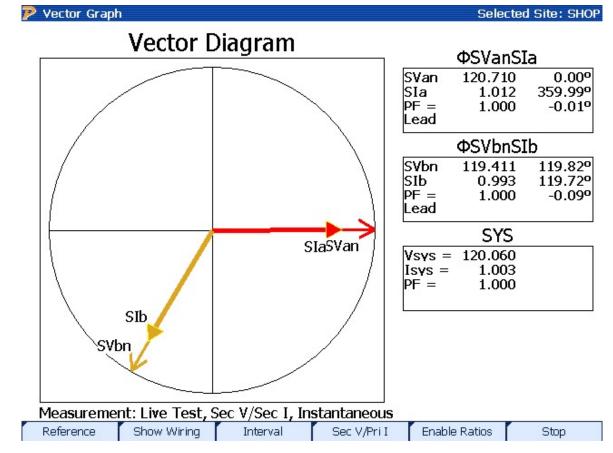


Two voltage sources with their returns connected to a common point. Provides 208 rather than 240 volts across "high side" wires.



2 Phase, 3-Wire "Network" Service

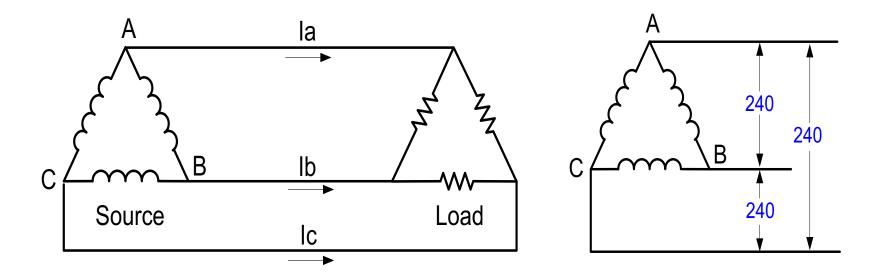
- Two Voltage Phasors
- 120° Apart
- Two Current Phasors
- Aligned with Voltage at PF=1





3 Phase, 3-Wire Delta Service

Common service type for industrial customers. This service has NO neutral.



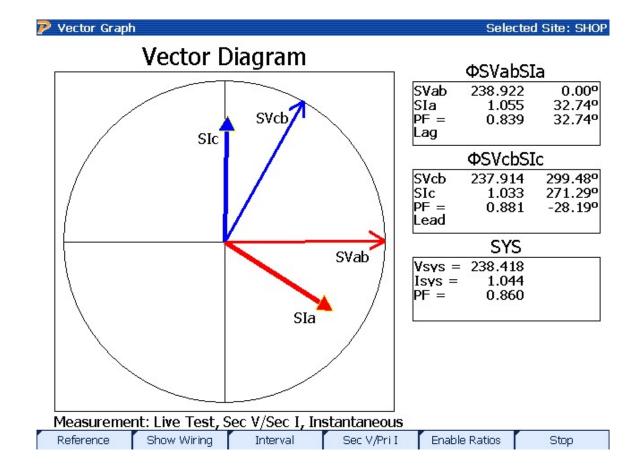
•Voltages normally measured relative to phase B.

- •Voltage and current vectors do not align.
- •Service is provided even when a phase is grounded.



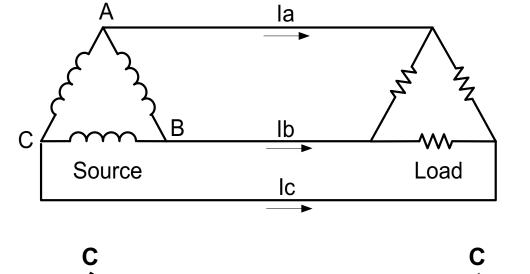
3 Phase, 3-Wire Delta Service Resistive Loads

- Two Voltage Phasors
- 60° Apart
- Two Current Phasors
- For a resistive load one current leads by 30° while the other lags by 30°





3 Phase, 3-Wire Delta Service Understanding the Diagram

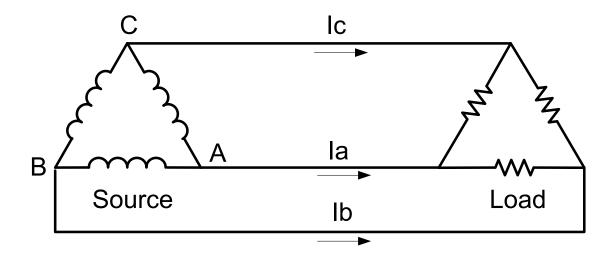


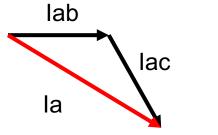


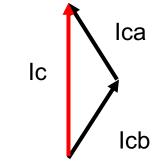


3 Phase, 3-Wire Delta Service

Understanding the Diagram





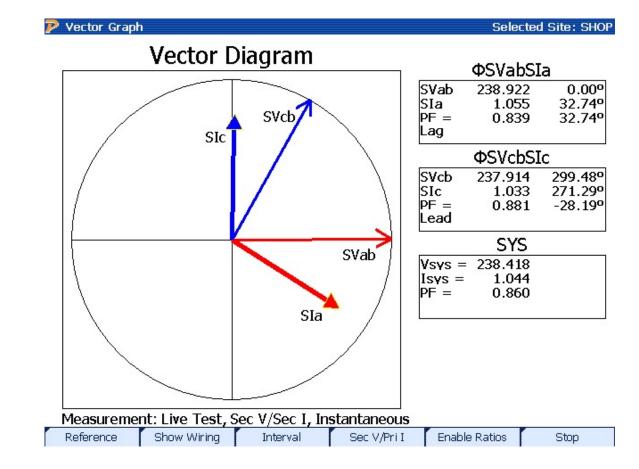




3 Phase, 3-Wire Delta Service

Resistive Load

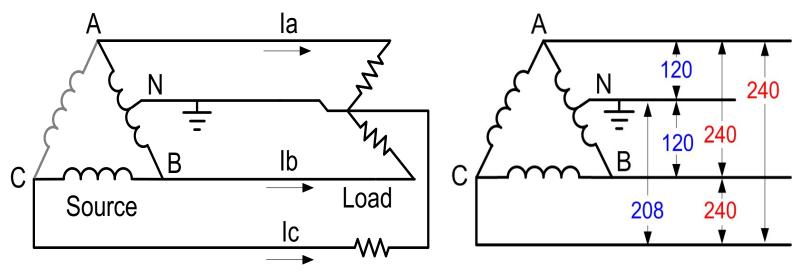
- Two Voltage Phasors
- 60° Apart
- Two Current Phasors
- For a resistive load one current leads by 30° while the other lags by 30°





3 Phase, 4-Wire Delta Service

Common service type for industrial customers. Provides a residential like 120/240 service (lighting service) single phase 208 (high side) and even 3 phase 240 V.



•Voltage phasors form a "T" 90° apart

•Currents are at 120° spacing

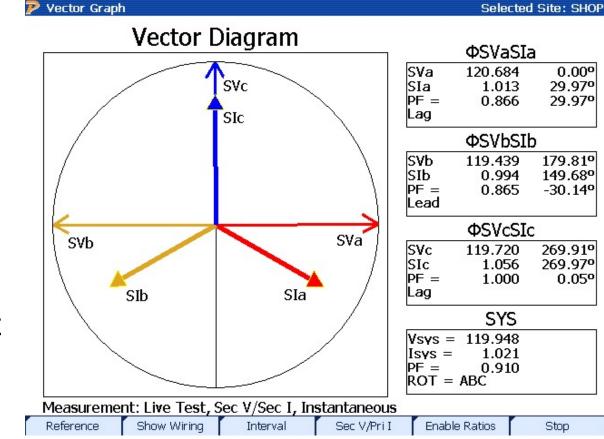
•In 120/120/208 form only the "hot" (208) leg has its voltage and current vectors aligned.



3 Phase, 4-Wire Delta Service

Resistive Load

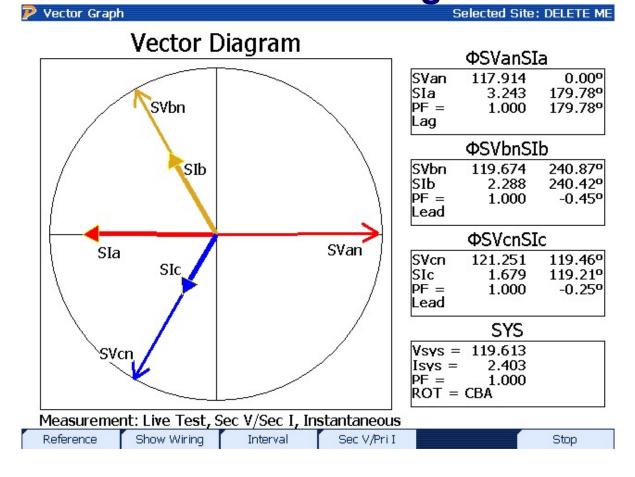
- Three
 Voltage
 Phasors
- 90° Apart
- Three Current Phasors
- 120° apart





Troubleshooting with Vectors

What's Wrong?



Phase A CT reversed.



Backwards CT = ??? \$\$\$

 kW = Va * Ia * Cos θ + Vb * Ib * Cos θ + Vc * Ic * Cos θ

 Cos 180 on phase A makes this NEGATIVE power!

 Reading will be 66% low assuming a balanced current load!



Troubleshooting with Vectors

What's Wrong?

Vector Graph Selected Site: DELETE ME Vector Diagram ΦSVanSIa SVan 118.017 0.000 SIa 240.46° 2.289 SVbn PF =0.493 -119.54º Lead ΦSVbnSIb SIa SVbn 119.774 240.91° SIP 3.245 359.770 PF =0.482 118.86° Lag ΦSVcnSIc SIbWan SVcn 121.387 119.50° SIC SIC 1.680 119.240 PF =1.000-0.26° Lead SYS Vsys = 119.726SVcn 2.405 Isvs = PF =0.658 ROT = CBAMeasurement: Live Test, Sec V/Sec I, Instantaneous Reference Show Wining Interval Sec V/Pri I Stop

Phase A & B CTs swapped.



Swapped Wire = ??? \$\$\$

 kW = Va * Ia * Cos θ + Vb * Ib * Cos θ + Vc * Ic * Cos θ

• Cos 120 on phase A and B makes this NEGATIVE power!

 Reading will be 0W assuming a balanced current load!



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Thank you for your time!



